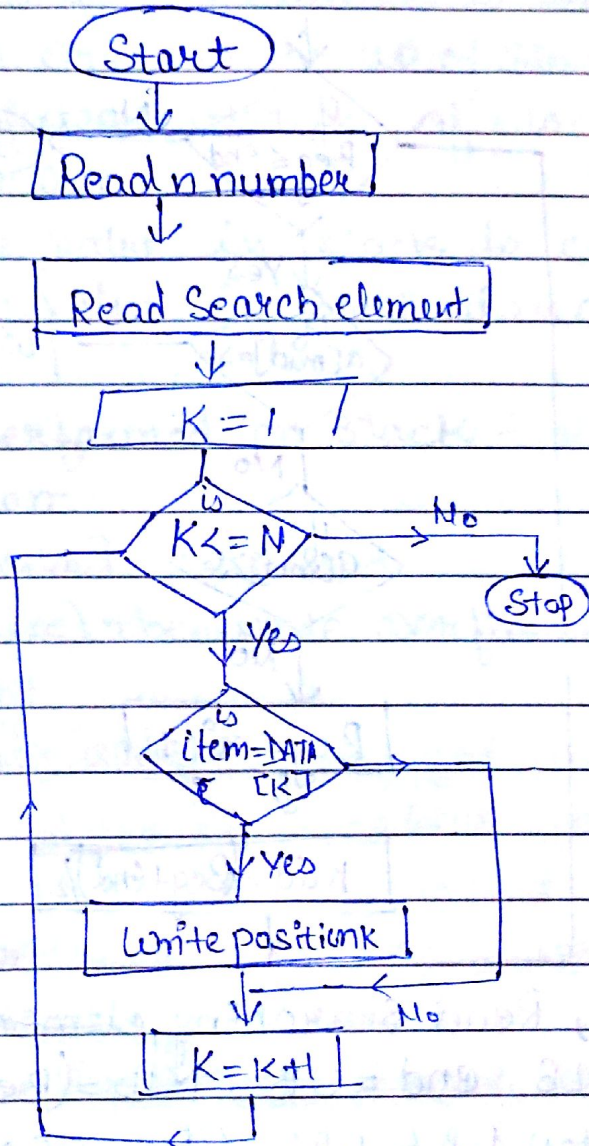


Searching: Searching can be done in two way

- 1) Linear Search
- 2) Binary Search

1) Linear Search:

Flow Chart:



Algorithm: Read n number, Read Search element

Step II: ^[initialize] Set $K := 1$

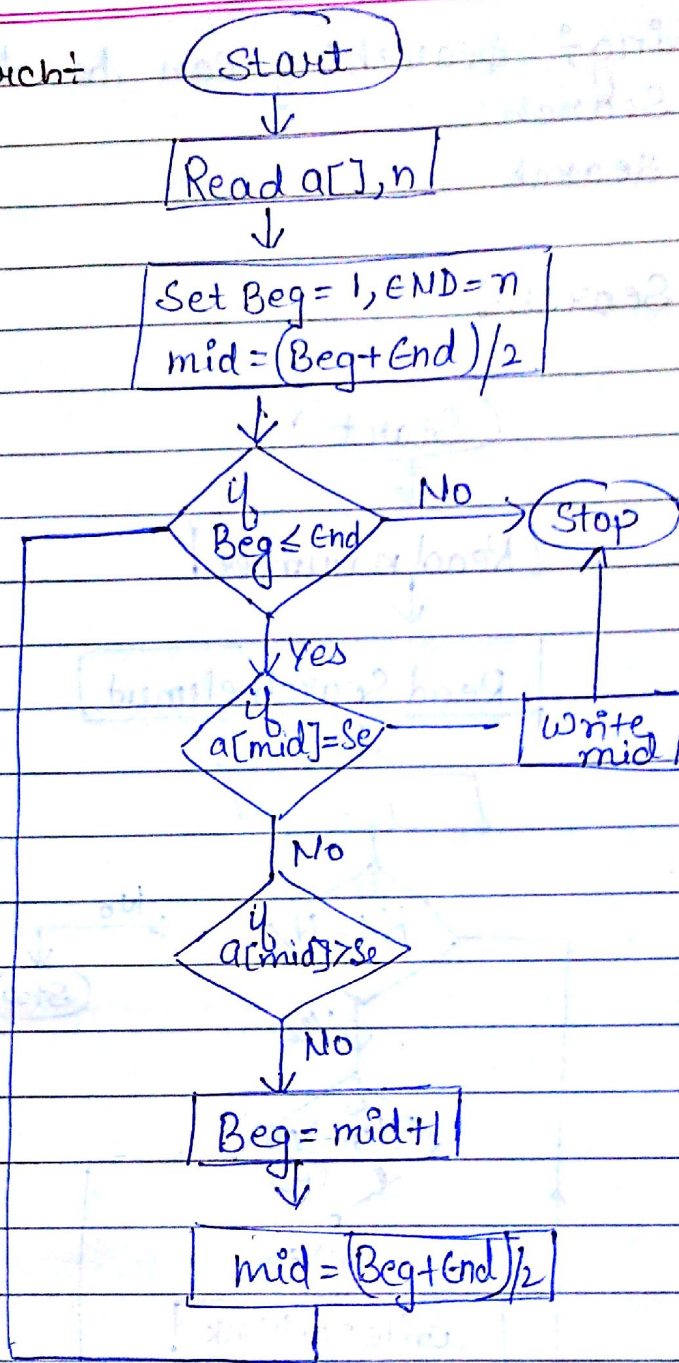
Step III: Repeat Step 4 & 5 while $K \leq N$

Step IV: [Comparison] If $(DATA[K] == item)$ then write position K

Step V: [Increment Counter] $K = K + 1$
[End of loop]

Step VI: Exit

2) Binary Search:



- Algorithm:
- Step I: Read n no, Read searching element
 - Step II: Set Beg = LB, end = UB, MID = (Beg + END) / 2
 - Step III: Repeat step 4 & 5 while (Beg <= END & a[mid] ≠ se)
 - Step IV: [Text Counter]
 - if (a[mid] > se) then
 - END := MID - 1
 - Else
 - Beg = MID + 1
 - Step V: MID = $\frac{Beg + END}{2}$ [End of Step 3 loop]

- Step VI: If $(a[mid] == se)$ then write Element position & exit the not found & exit
- Step VII: Exit

Stack: Stack is a non primitive linear data structure in which insertion and deletion is done only at one end of the stack or the top of stack. It is called sequential representation of stack. It is LIFO Last in First out

Inserting the value in stack is called Push
Deleting the value in stack is called pop.

Operation performed on stack :-

1) Push operation:-

- Step 1: Set stack[size]
- Step 2: If $(Top == Size)$ then write overflow & exit
- Step 3: $Top = Top + 1$
- Step 4: $Stack[Top] = item$
- Step 5: Exit

2) Pop operation:-

- Step 1: Set stack[size]
- Step 2: If $(Top == 0)$ then write underflow & exit
- Step 3: $item = Stack[Top]$
- Step 4: $top = top - 1$
- Step 5: Go to Step 2

Mathematic Expression:-

- 1) Infix: In which the operator symbol is placed between its two operands
eg $A + B$
 $C * D$

2) Prefix Notation \div eg $+AB$, $*CD$. Referred to the notation in which the operator symbol is placed before its two operands. It is also called the polish notation.

3) Postfix Notation | Reverse polish Notation \div It is referred to the notation in which the operator symbol is placed after its two operands eg $AB+$, $CD-$

Evaluation of postfix expression

ALGORITHM: Add a right parenthesis ")" at the end of Expression (P)

Step 2: Scan P from Left to Right & repeat step 3 & 4 for each element of p until ")" is encountered.

Step 3: If an operand is encountered put it on stack

Step 4: If an operator \otimes is encountered then

(a) Remove the top element of stack, where A is the top and B is next to top element

(b) Evaluate $B \otimes A$

(c) place result of (b) on stack

Step 5 Set value equal to top element

Step 6 Exit

Conversion of Infix to postfix:

ALGORITHM: Let Q be an arithmetic operation written in infix notation. This algorithm finds the equivalent expression into postfix expression

Step 1: Push "(" on to stack and ")" to the end of Q

Step 2: Scan Q from Left to Right & repeat step 3 to 6 from element Q until the stack is empty

- Step 3 If an operand is encountered, add it to p
- Step 4: If an left paranthesis "(" is encountered, push it to stack
- Step 5: If an \otimes operator is encountered then
- Repeatedly pop from stack & add to p each operator which has the same or high precedence than \otimes
 - Add \otimes to stack.
- Step 6: If an right paranthesis ")" is encountered then
- Repeatedly pop from stack & add to p each operator until a left paranthesis is encountered
 - Remove the left paranthesis
- Step 7 Exit

Queue: A Queue is a non primitive linear data structure it is a homogeneous collection of element in which element are added at one end called rear; and existing element are deleted from the other end called front. Queue are also called First in First out (FIFO)

Inserting the element from Queue:

- ALGORITHM:- Set the size of Queue, Queue [n];
- Step 2 Initialize front = 0, Rear = 0
- Step 3 If $Rear \geq n$ (max size) [check overflow]
Write Queue overflow & return
- Step 4 $Rear = Rear + 1$
- Step 5 $Queue[Rear] = item$
- Step 6 Return

Deleting the element from Queue:

ALGORITHM: If front = 0 or NULL then write Queue is empty [underflow] & exit

Step 2 item = Queue [front]

Step 3 front = front + 1

Step 4 Go to Step 1

Link List: It is one way list. It consist of Nodes which has two part information and address part contain address of next node and end of linklist is contain a Null pointer

Insertion at beginning

Step: ① Check to see if free space is available in avail list

If Avail = null the print link list overflow

② Remove the first node from the avail list using the variable new to keep track of the location of the new node this stmt can be implemented by

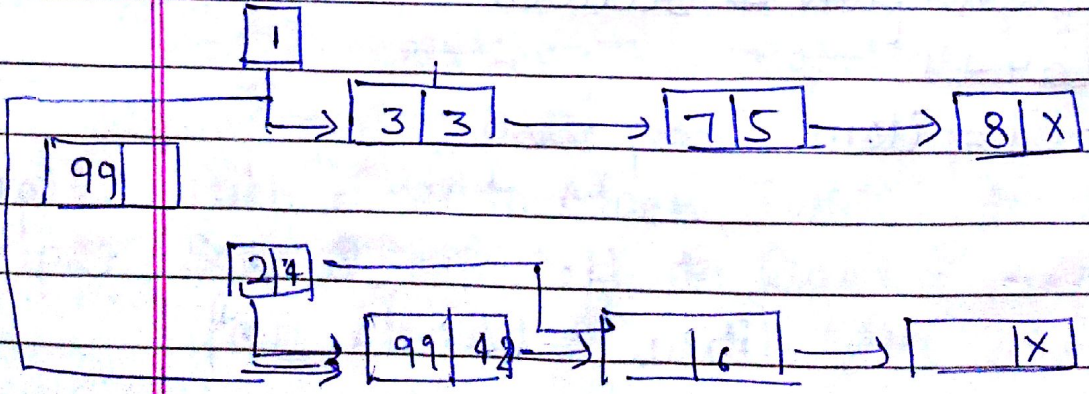
$$New = Avail$$

$$Avail = Link[Avail]$$

③ copy new information into new node this can be implemented as

$$info[new] = item$$

start



ALGORITHM: [Overflow] If Avail = NULL then write overflow and exit

- Step 1: [Remove first node from avail list]
set New := Avail, Avail = Link [new]
- Step 2: set info [new] = item [copies new data]
- Step 3: set Link [new] = start [new node now points to original first node]
- Step 4: set start = new [changes start to new points to original new node]
- Step 5: Exit

Insertion at middle

- Step 1: [Overflow] If avail = NULL then write overflow and exit
- Step 2: [Remove first node from list]
set New := Avail and Avail = Link [Avail]
- Step 3: set Info [New] = item
- Step 4: If LOC = NULL then [Insert at first node]
set Link [new] = Start and start = new
else [insert after node with location]
- Step 5: set LINK [New] = LINK [LOC] & LINK [LOC] = new
- Step 6: Exit

Deletion at middle:

- Step 1: If LOCP = NULL then START = Link [start]
else set LINK [LOCP] = LINK [LOC]
- Step 2: [Returned Deleted node to avail]
set LINK [LOC] := Avail & Avail = Loc
- Step 3: Exit

Sorting :-

Bubble Sort :-

eg :-

4	3	3	3	3	1
3	4	4	4	1	3
5	5	5	1	4	4
10	10	10	5	5	5
1	10	10	10	10	10

ALGORITHM

① [Initialization] Read $a[i]$, n

Step Set $i = 1$

② Repeat step 3, 4 while $j \leq n-1$

③ Repeat step 4 while $i \leq n$

④ If $a[i] > a[i+1]$

then swap = $a[i]$

$a[i] = a[i+1]$

$a[i+1] = \text{swap}$

⑤ end of 5 step, 4 step & 3 step

⑥ Print the Stmt

⑦ exit

Insertion Sort

eg

10	9	8	7	6	5
9	10	8	7	6	5
8	8	10	7	6	5
11	11	11	10	6	5
7	7	7	11	6	5
6	6	6	6	11	5
5	5	5	5	5	11

ALGORITHM Set $A[0] = -\infty$

② Repeat step 3 to 5 for $k = 2, 3, \dots, n$

③ Set $TEMP = A[k]$ and $PTR = k-1$

④ Repeat while $TEMP < A[PTR]$

(a) Set $A[PTR+1] = A[PTR]$

(b) Set $PTR := PTR - 1$

[End of loop]

Set $A[PTR+1] = TEMP$

[End of step 2 loop]

(c) Return

Selection Sort ↴

① Repeat step 2 and 3 for $K = 1, 2, \dots, N-1$

② Call $MIN(A, K, N, Loc)$

③ [Interchange $A[K]$ and $A[Loc]$]

Set $TEMP = A[K]; A[K] = A[Loc]$ and $A[Loc] = TEMP$

End of Step 1 loop

④ Exit

→ ALGORITHM ÷ It is a well define computational procedure that take some value or set of value as input and produces some values or set of values as output

An algorithm is a sequence of computational steps that transforms the input into the output

Factor to decide the Best Algorithm ÷

① No of item to be sorted

② Input values are already sorted

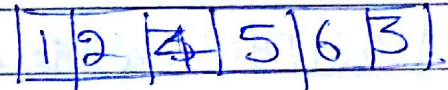
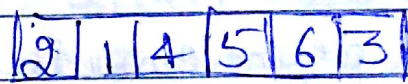
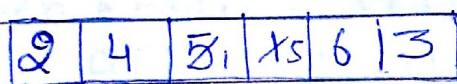
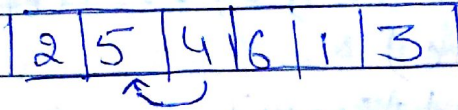
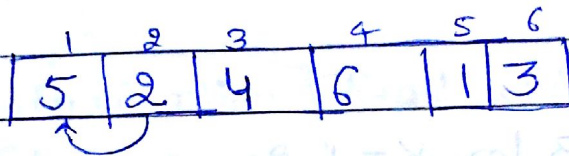
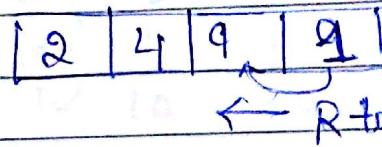
③ Architecture of the computer and the kind of storage devices we used

④ An algorithm is set to be correct for every input instance, it hold with correct output which solve

Computational problem
⑤ An incorrect algorithm might not fault at all on some, instances or it might and with an incorrect answers

→ Data Structure :- It is a way to store organised data in order to facilitate access and modification.

Insertion Sort :- Easiest sorted method



eg 31 41 59 26 41 58

31 41 26 59 41 58

31 26 41 59 41 58

26 31 41 59 41 58

26 31 41 41 59 58

26 31 41 41 58 59

Algorithm :-

1) for $j = 2$ to A length

2) Key = $A[j]$

3) // Insert $A[j]$ into sorted sequence $A[1 \dots j-1]$

4) $i = j - 1$

5) while $i > 0$ and $A[i] > \text{Key}$

- 6) $A[i+1] = A[i]$
- 7) $i = i-1$
- 8) $A[i+1] = \text{key}$

Analysis :-

Cost	times
C_1	n
C_2	$n-1$
C_4	$n-1$
C_5	$\sum_{j=2}^n t_j$
C_6	$\sum_{j=2}^n t_j - 1$
C_7	$\sum_{j=2}^n t_j - 1$
C_8	$n-1$

$$T(n) = C_1 n + C_2(n-1) + C_4(n-1) + C_5 \sum_{j=2}^n t_j + C_6 \sum_{j=2}^n (t_j - 1) + C_7 \sum_{j=2}^n (t_j - 1) + C_8(n-1)$$

$$= C_1 n + C_2 n - C_2 + C_4 n - C_4 + C_5(n-1) + C_8(n-1)$$

$$= \textcircled{n}(C_1 + C_2 + C_4 + C_5 + C_8) - (C_2 + C_4 + C_5 + C_8)$$

\neq complexity.

This running time as $an + b$ for constants a & b that depend upon statement cost C_i is a linear function of N

If array is in the reverse order. If we must compare each element array $[j]$ with

each element in the entered subarray $a[1]$ to $a[j-1]$ and so $t_j = j$ for $2, 3, 4, \dots, n$

$$1 + 2 + 3 + \dots + n - 1$$

$$C_5 = \frac{n(n+1)}{2} - 1$$

$$C_6 = \sum_{j=2}^n (j-1) = \frac{n(n-1)}{2}$$

$$1 + 2 + 3 + 4 + \dots + (n-1) + n - n$$

$$= \frac{n(n+1)}{2} - \frac{n}{1}$$

$$= \frac{n(n+1) - 2n}{2} = \frac{n^2 + n - 2n}{2} = \frac{n^2 - n}{2}$$

$$= \frac{n(n-1)}{2}$$

$$T(n) = C_1 n + C_2(n-1) + C_4(n-1) + C_5 \left(\frac{n(n+1)}{2} - 1 \right)$$

$$+ C_6 \left(\frac{n(n-1)}{2} \right) + C_7 \left(\frac{n(n-1)}{2} \right) + C_8(n-1)$$

$$= n(C_1 + C_2 + C_4) - (C_2 + C_4) + C_5 \left(\frac{n^2 + n - 2}{2} \right) + \frac{C_6 n^2 - C_6 n}{2}$$

$$+ \frac{C_7 n^2 - C_7 n}{2} + C_8 n - C_8$$

$$= n^2 \left(\frac{C_5}{2} + \frac{C_6}{2} + \frac{C_7}{2} \right) + n \left(C_1 + C_2 + C_4 + C_8 + \frac{C_5 - C_6}{2} - \frac{C_7}{2} \right)$$

$$- (C_2 + C_4 + C_5 + C_8)$$

$$ax^2 + bx + c$$

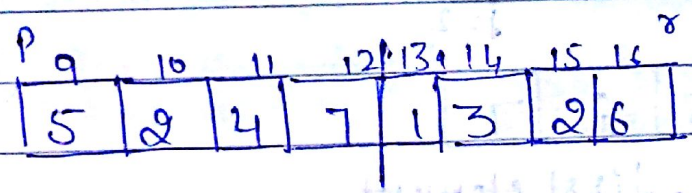
We can express this worst case running time as $ax^2 + bx + c$ for constant a, b, c that again depend upon statement cost COS . It is a quadratic function of n .

Divide and Conquer approach:

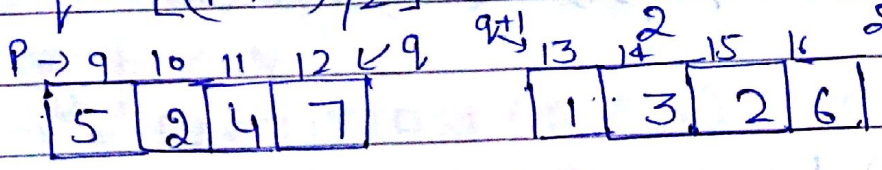
- Divide
- Conquer
- Combine

Some Algorithms are recursive in structure to solve a given problem they call themselves recursively one or more times to deal with closely related some programs.

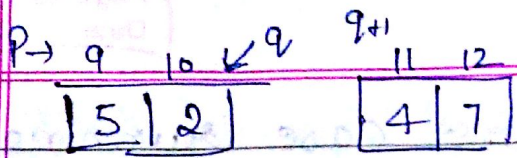
These Algorithms follow a divide and conquer approach. They break a program into several such programs that are similar to original problem but small in size. Solve the sub problem recursively then combine this solution to create a solution to original program.



$$q = \lfloor (p+r)/2 \rfloor = \lfloor (9+16)/2 \rfloor = \lfloor 25/2 \rfloor = \lfloor 12.5 \rfloor = 12$$



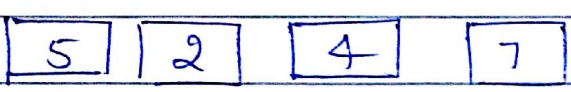
$$\lfloor \frac{(p+q)}{2} \rfloor = \lfloor \frac{9+12}{2} \rfloor = \lfloor \frac{21}{2} \rfloor = \lfloor 10.5 \rfloor = 10$$



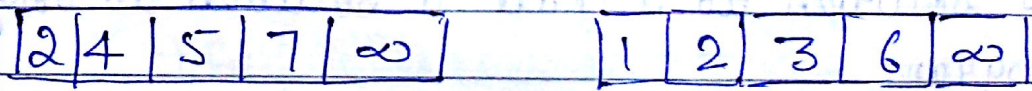
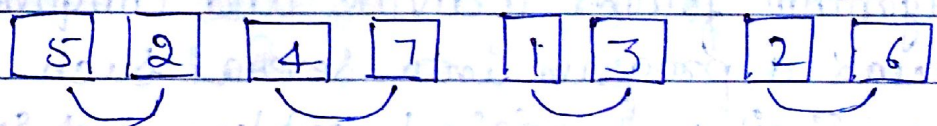
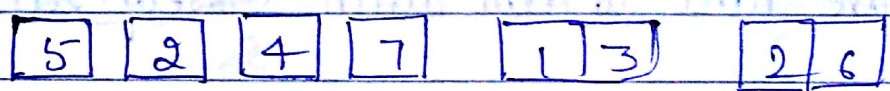
$$\left\lfloor \frac{9+10}{2} \right\rfloor = \left\lfloor \frac{19}{2} \right\rfloor = \left\lfloor 9.5 \right\rfloor = 9$$



$$\left\lfloor \frac{11+12}{2} \right\rfloor = \left\lfloor \frac{23}{2} \right\rfloor = \left\lfloor 11.5 \right\rfloor = 11$$

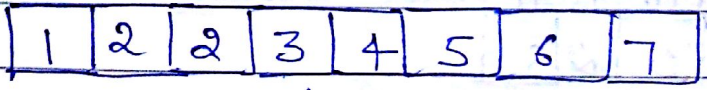


$$\left\lfloor \frac{13+16}{2} \right\rfloor = \left\lfloor \frac{29}{2} \right\rfloor = \left\lfloor 14.5 \right\rfloor = 14$$



$i=1$

$j=1 \downarrow$
 $j=2$



away first element

Algorithm: Merge sort (A, P, R) last element = R

1) if $p < r$

2) $q = \left\lfloor \frac{p+r}{2} \right\rfloor$

3) MERGE SORT (A, P, q)

4) MERGE SORT (A, q, R)

Combine 5) MERGE (A, p, q, r)

- | | |
|--|--------------------------------|
| 1) $n_1 = q - p + 1$ | $\Rightarrow (12 - 9 + 1) = 4$ |
| 2) $n_2 = r - q$ | $= (16 - 12) = 4$ |
| 3) let $L[1 \dots n_1 + 1]$ and $R[1 \dots n_2 + 1]$ be new arrays | |
| 4) for ($i = 1$ to n_1) | ($i = 1$ to 4) |
| 5) $L[i] = A[p + i - 1]$ | $A[9 + 1 - 1] = 9$ |
| 6) for ($j = 1$ to n_2) | ($j = 1$ to 4) |
| 7) $R[j] = A[q + j]$ | $A[12 + 1] = A[13]$ |
| 8) $L[n_1 + 1] = \infty$ | $L[4 + 1] = 5$ |
| 9) $R[n_2 + 1] = \infty$ | $R[4 + 1] = 5$ |
| 10) $i = 1$ | $i = 1$ |
| 11) $j = 1$ | $j = 1$ |
| 12) for $k = p$ to r | $k = 9$ to 16 |
| 13) if $L[i] \leq R[j]$ | $L[1] \leq R[1]$ |
| 14) $A[k] = L[i]$ | $A[9] = L[1]$ |
| 15) $i = i + 1$ | $i = 1 + 1 = 2$ |
| 16) else $A[k] = R[j]$ | $A[9] = R[1]$ |
| 17) $j = j + 1$ | $j = 1 + 1 = 2$ |

Quick sort: Application of Divide and Conquer

i	p	q	r	s	t	u	v	w	x
	2	8	7	1	3	5	6	4	

Algorithm: QuickSort(A, p, r)

- 1) if $p < r$
- 2) $q = \text{PARTITION}(A, p, r)$
- 3) QuickSort(A, p, q)
- 4) QuickSort(A, q+1, r)
- 5) PARTITION(A, p, r)
- 6) $x = A[r]$ // $x = 4$

$i = p - 1; \Rightarrow i = 0$

for $j = p$ to $x - 1$

if $A[j] \leq x$

$i = i + 1$

Exchange $A[i]$ with $A[j]$

Exchange $A[i + 1]$ with $A[x]$

return $i + 1$

for ($j = 1; j \leq 7; j++$)
{
if ($A[j] \leq x$)
{
 $i = i + 1$
Swap $A[i]$ & $A[j]$
}}}

