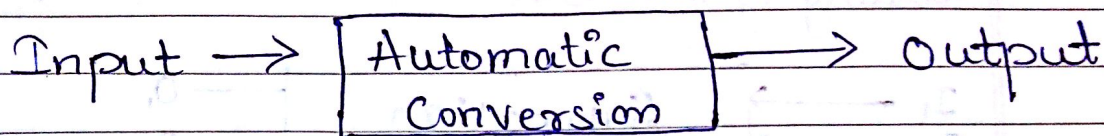


Theory of Automata and Computation



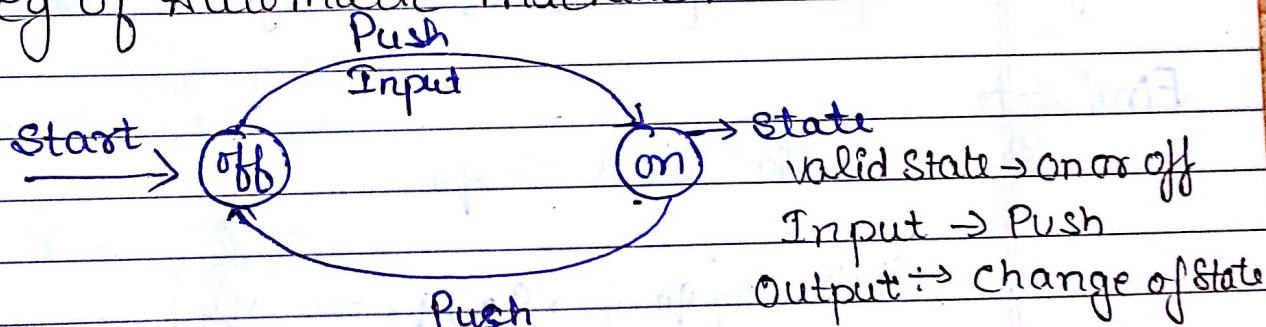
Language

a, b

Grammar Rules

- ① b after a
- ② Starting Symbol a

Eg of Automatic machine :-

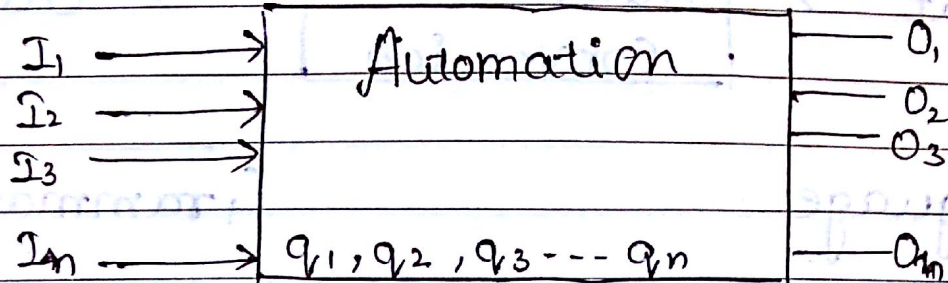


Defination of Automation:-

An Automation is defined as a System where energy, materials and information are transferred transformed and used for performing some functions without direct participation of man eg are Automatic machine Tools, Automatic washing machine

- 1) All finite states of an Automation are represented by a circle
- 2) Input of the system are represented by arc. It shows the external influence on the system
- 3) One of the state is designated the start state

The State in which the system is placed initially. It is indicated by the word Start and an arrow leading to that State.



Model of Discrete Automation

alphabet

- Denoted by Σ ① Input $\rightarrow \{I_1, I_2, I_3, I_4, \dots, I_n\} \rightarrow \text{finite}$
 Q ② Valid state $\rightarrow \{q_1, q_2, q_3, \dots, q_n\}$
 Denoted by f ③ Output $\rightarrow \{O_1, O_2, O_3, \dots, O_n\} \rightarrow \text{limited}$

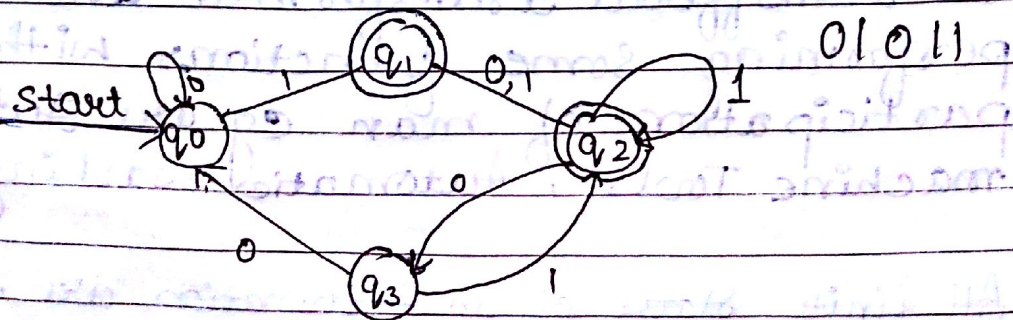
Final state

- ④ Initial state $\rightarrow q_0$

State $\rightarrow \{q_0, q_1, q_2, q_3, \dots, q_n\}$

- ⑤ $\delta \rightarrow \text{transiting function}$

$$M = \{Q, \Sigma, q_0, f, \delta\}$$



$$Q = \{q_0, q_1, q_2, q_3\}$$

$$\Sigma = \{0, 1\}$$

Initial State $\rightarrow q_0$

Final State $\rightarrow \{q_1, q_2\}$

$\delta \rightarrow Q \times \Sigma \rightarrow Q$

$q_0 \times 0 \rightarrow q_0$

$q_0 \times 1 \rightarrow q_1$

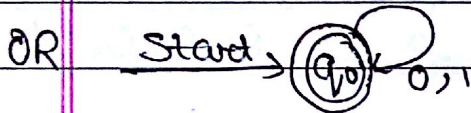
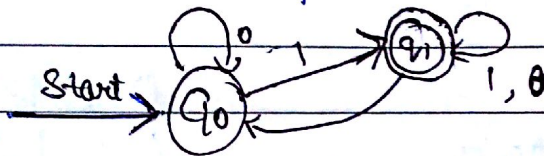
$q_1 \times 0 \rightarrow q_2$

$q_2 \times 1 \rightarrow q_2 \rightarrow$ we check this state if it is final state then it accept the input

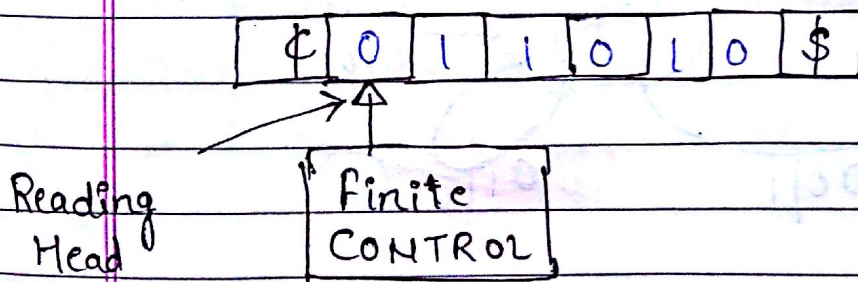
Regular Expression $\rightarrow$ eg 000011111 then it

Regular Expression is 0^*1^*

Machine for 0^*1^*



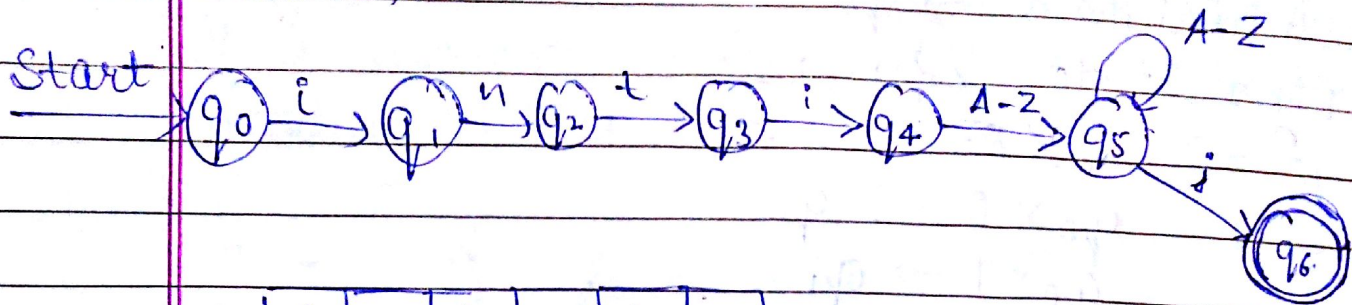
$\rightarrow$ Finite automaton, DFA automaton



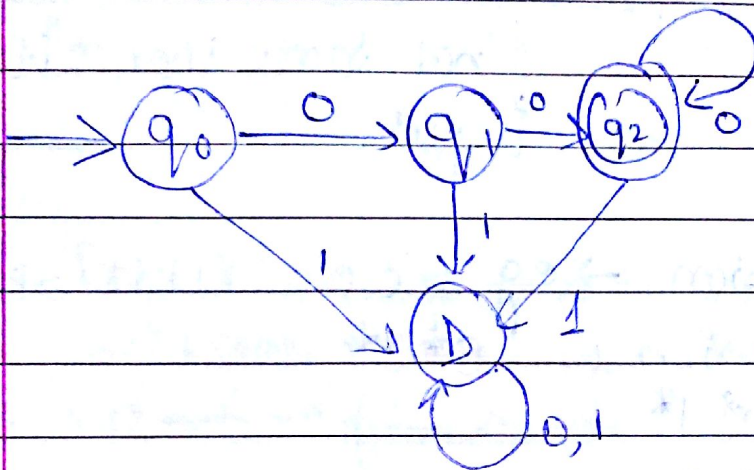
Block Diagram of a Finite Automaton

States $= \{q_0, q_1\}$
 $\Sigma = \{0, 1\}$

int i; i=0



i n t i ;

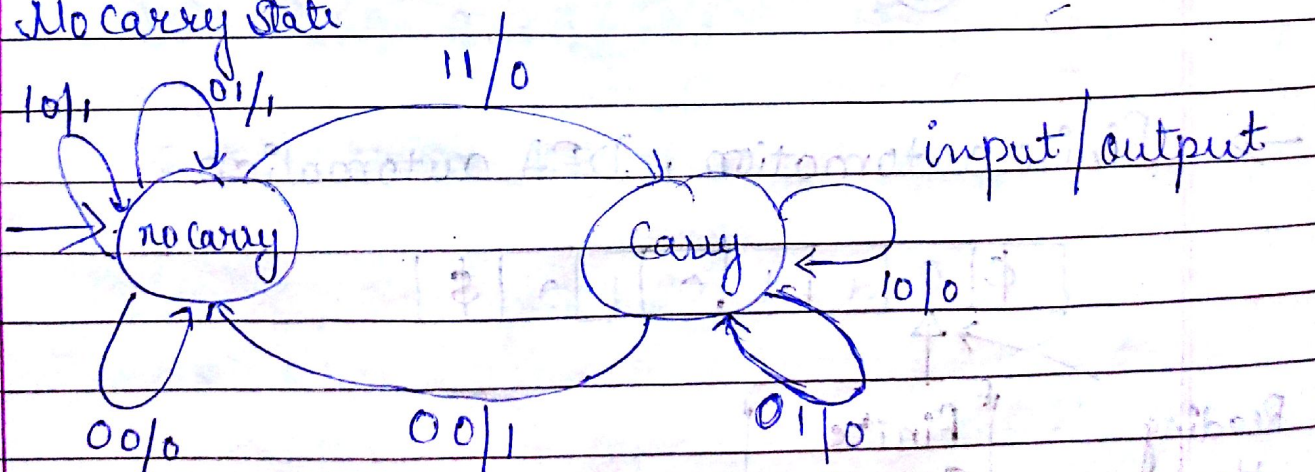


System Check two state

- 1) Carry state
- 2) No carry state

0 1 1 1 0
 0 0 1 0 1

 0 0 0 1 1



$\Sigma = \{0, 1\}$
 $L(M) = \{00, 10, 01, 11\}$
 output = $\{0, 1\}$

Central Concepts of Automata Theory :

- 1) Alphabets (Set of Symbols) $\Sigma = \{0, 1\}$
- 2) Strings (List of Symbols from an alphabet)
- 3) Language (Strings from same alphabet)

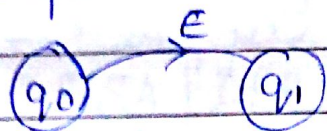
These concepts include alphabets, strings & language

1) Alphabet: It is a finite non empty set of Symbol denoted by Σ eg $\Sigma = \{0, 1\}$ it is eg of Binary set

eg $\Sigma = \{a, b, c, \dots, z\}$ it is a set of lower case letters

2) String: A string is a finite sequence of Symbols chosen from some alphabet (Σ) sigma
eg 01101 is a string from the Binary alphabet
 $\Sigma = \{0, 1\}$

• Empty string: It is defined as a string with zero occurrences of symbols. This string denoted as ϵ is a string that may be chosen from any alphabet.



• Length of a string: Strings are classified by their length. Length means no. of positions for symbols in a string. The standard notation for the length of string is denoted as w
eg $w = \{1100011\}$

$$|w| = 7$$

$$|\epsilon| = 0$$

The length of string $|w|$ is 7.

- Powers of an alphabet (Σ): If Σ is an alphabet we can express the set of all strings of a certain length from that alphabet by using an exponential notation

Σ^K where K is an integer where $K=3$
 eg: $\Sigma^3 = \{000, 001, 101, 010, 110, \dots, 111\}$

$$\Sigma^0 = \{\epsilon\}, \Sigma^* = \Sigma^0 \cup \Sigma^1 \cup \Sigma^2 \cup \Sigma^3 \dots \Sigma^n$$

$$\Sigma^+ = \Sigma^1 \cup \Sigma^2 \cup \Sigma^3$$

- Concatenation of String:

$$x = 01101, y = 0011 \rightarrow xy = 011010011$$

- 3) Languages: A set of strings all of which are chosen from some Σ^* , where Σ is a particular alphabet is called language.
- If L is a language and Σ is alphabets and language is a subset of alphabets
- $$L \subseteq \Sigma^* \text{ over } \Sigma$$
- $$L = \{\Sigma^*\}$$

Any language over Σ is also the language of any alphabets i.e. Superset of Σ

- Why we are using term language?

Because every language can be viewed as set of strings.

eg: $\Sigma = \{a, b, c, \dots, z\}$

L is English $L \subseteq \Sigma^*$

English is collection of legal english word is a set of string over the alphabets that consists of all the 26 letter

C-language + legal program are subset of the possible string that can be formed from the alphabets of the language
This alphabet is subset of ASCII

$\emptyset \rightarrow$ Empty language is a language of over any alphabet

$\{\epsilon\} \rightarrow$ A language consisting of only the empty string

$$\emptyset \neq \{\epsilon\}$$

$\emptyset$ has no string $\{\epsilon\}$ has 1 string

NOTE: For any language alphabet are finite. A language can have an infinite no of string, are restricted to consist of string from one fixed finite alphabet.

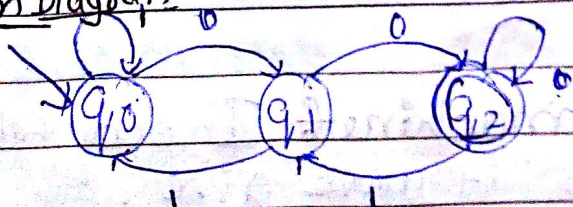
Assignment: Transition System

FSA / DFSA / DFA :

$$M = \{Q, \Sigma, \delta, q_0, F\}$$

$$M = \{H, \Sigma, \delta, H_0, F\}$$

Transition Diagram



$$Q = \{q_0, q_1, q_2\}$$

$$\Sigma = \{0, 1\}$$

$$\delta = Q \times \Sigma \rightarrow Q$$

Initial State q_0

$$F = \{q_2\}$$

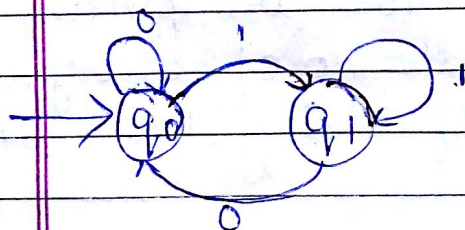
Transition Table:

	Input	
	0	1
State q_0	q_1	q_0
q_1	q_2	q_0
Final state q_2 *	q_2	q_1

eg:

State	0	1
q_0	q_0	q_1
q_1	q_0	q_1

Diagram:

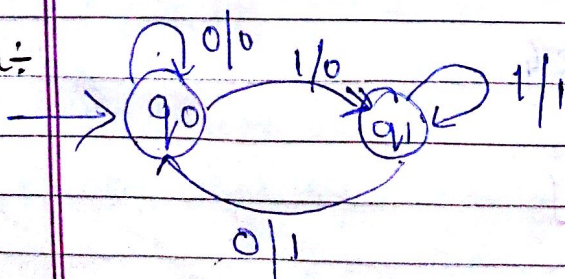


eg →

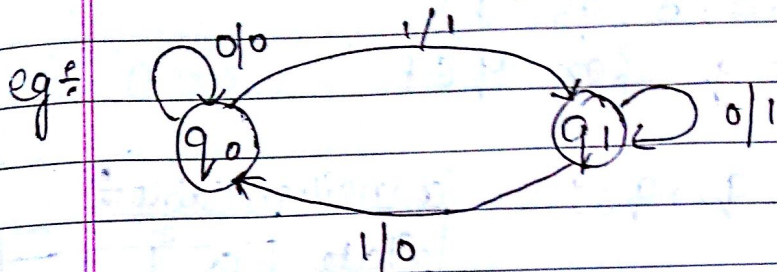
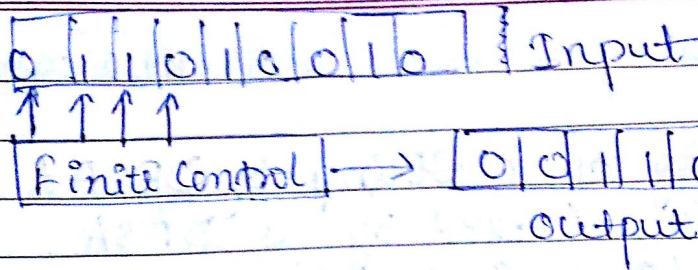
Input → 01101001

Output → 00110100

Given:



One moment delay machine: Input which it take the ^{same} output it gave give.
It start from zero



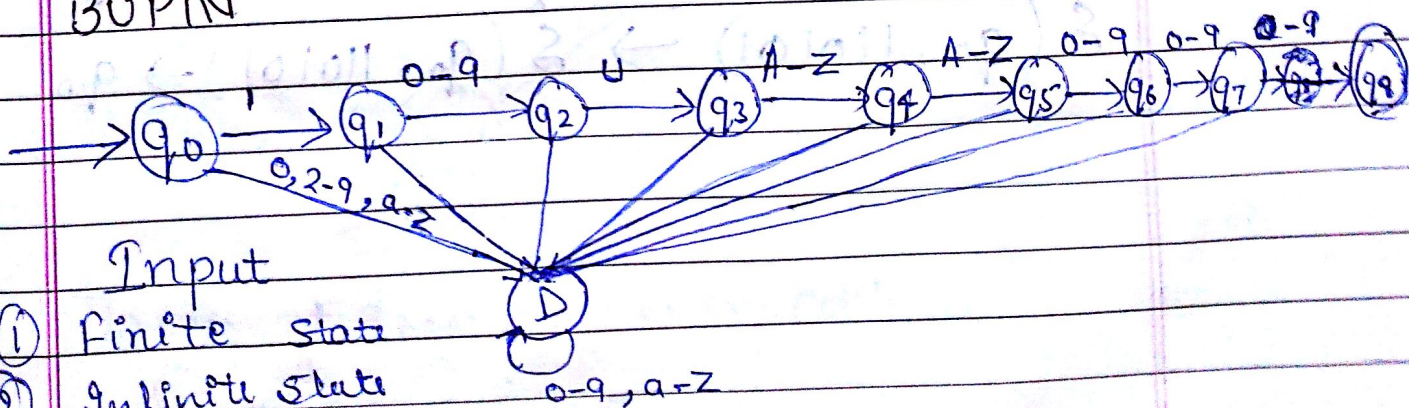
State	0	1
q ₀	q ₀ 0	q ₁ 1
q ₁	q ₁ 0	q ₀ 1

Input → 1 1 0 0 1 1 0 1
Output → 1 0 0 0 1 0 0 1

If odd no. of ones in input then output of last is one i.e. is called parity checker and vice versa for even no. of ones in input then output of last is Zero

11UCS001

BU PIN



- Input
- Finite state
 - Infinite state

$$\Sigma = \{0-9, a-z\}$$

It is a string acceptor or BUPIN acceptor

Acceptability of a string by DFSA: A string w is accepted by a DFSA

$$M = (Q, \Sigma, \delta, q_0, F)$$

if $\delta(q_0, w) = q$ for $q \in F$

$$Q = \{q_0, q_1, q_2, q_3\}$$

$$\Sigma = \{0, 1\}$$

$$F = \{q_0\}$$

Transition table:

State	Σ	
	0	1
$\rightarrow q_0$	q_2	q_1
q_1	q_3	q_0
q_2	q_0	q_3
q_3	q_1	q_2

Input - 110101

$$\delta(q_0, 110101) \rightarrow \delta(q_1, 10101) \rightarrow$$

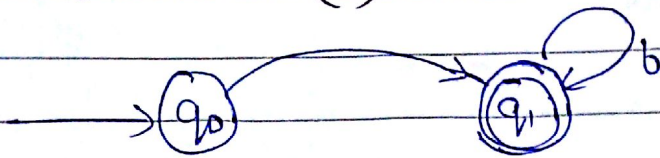
$$\delta(q_0, 0101) \rightarrow \delta(q_2, 101) \rightarrow \delta(q_2, 01)$$

$$\delta(q_1, 1) = q_0 \in F$$

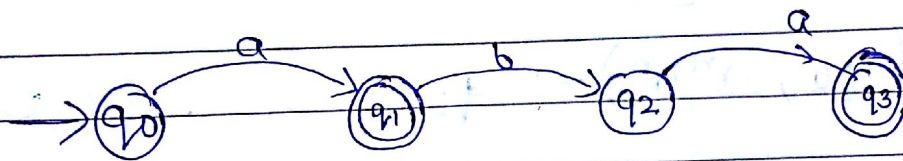
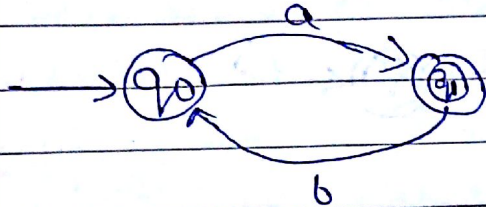
Hence this machine accept the string

$$\delta(q_0, 110101) \rightarrow \hat{\delta}(q_0, 110101) \rightarrow q_0$$

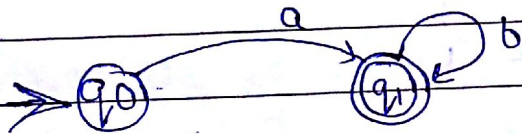
Eg: $ab^n \rightarrow a(b)^*$



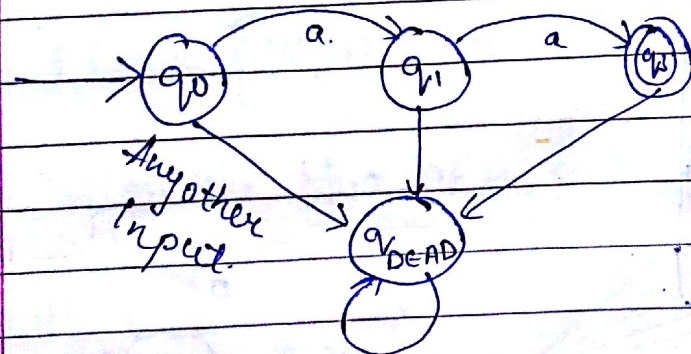
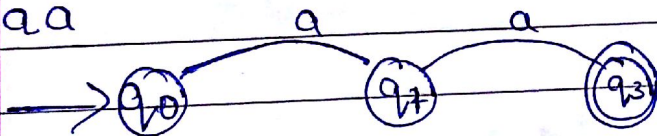
→ aba



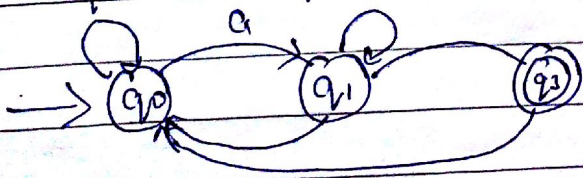
→ $ab^na \rightarrow a(b)^*a$

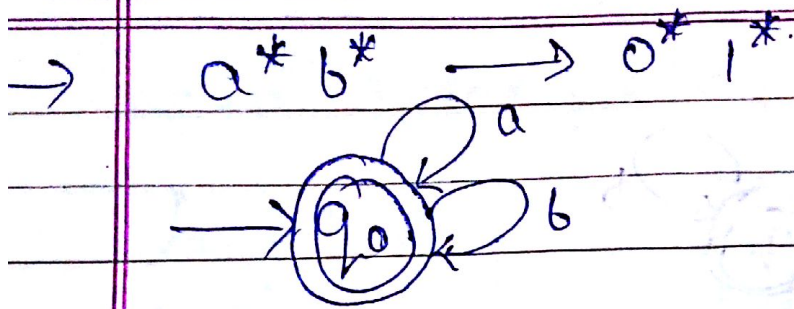


→ aa

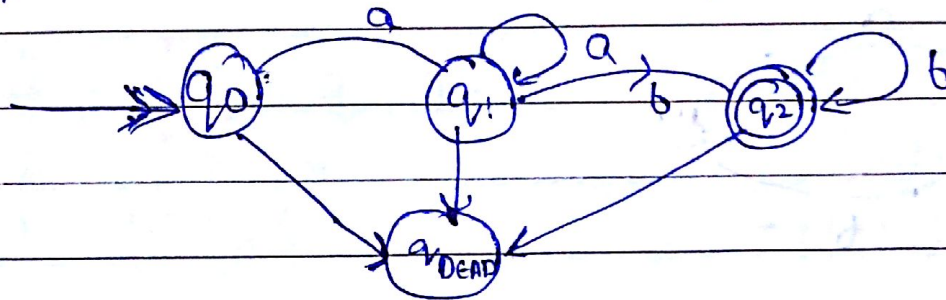


To prevent q_{DEAD} we use try catch



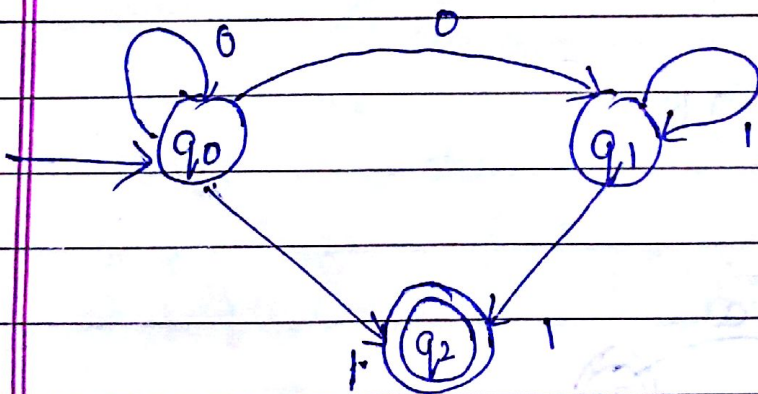


→ $a^n b^n, n \geq 0 \quad \Sigma^* = \{a, b\} \quad \Sigma^+, \Sigma^* \rightarrow 0$ occurs in



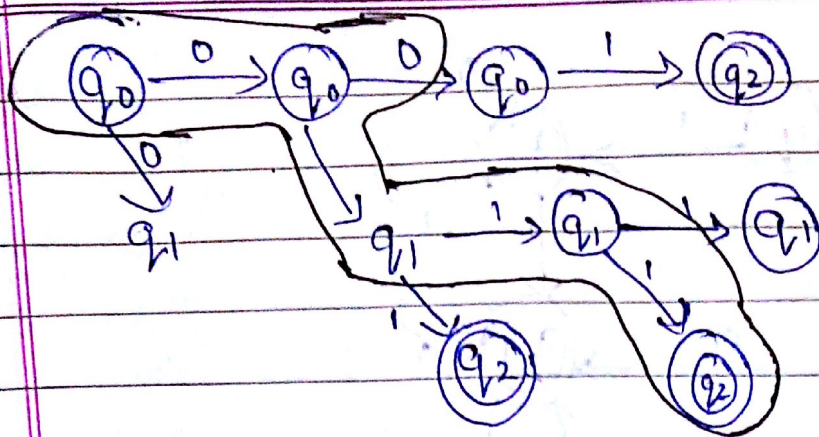
$\delta(q_0, a^n b^n) \rightarrow q_2$

NFSM (Non Deterministic Finite State Machine):



Transition Table:

State	0	1
→ q ₀	{q ₀ , q ₁ }	{q ₂ }
q ₁	∅	{q ₁ , q ₂ }
q ₂	∅	∅



0011

Some moves of the machine cannot be determined uniquely by the input symbol and the present state. Such machines are called Non Deterministic Finite automata.

$$M = \{Q, \Sigma, \delta, q_0, F\}$$

Non Deterministic machine

$Q \rightarrow$ set of state

$\Sigma \rightarrow$ input alphabet

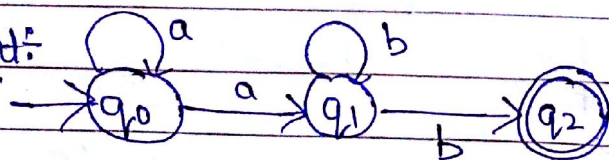
$\delta \rightarrow Q \times \Sigma \rightarrow 2^Q$ $p(Q)$

$$L(M) = \{w \mid w \in \Sigma^*\}$$

$$L(M) = \{w \mid w \in \Sigma^*, \delta(q_0, w) \rightarrow Q \cap F \neq \emptyset\}$$

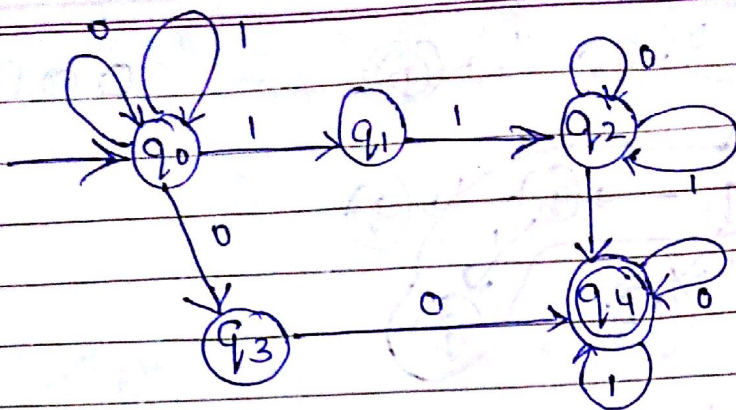
→ Difference b/w DFA & NDFA

Assignment:

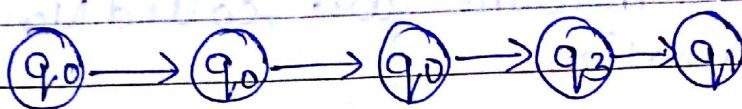


Input $\rightarrow$ aacabb

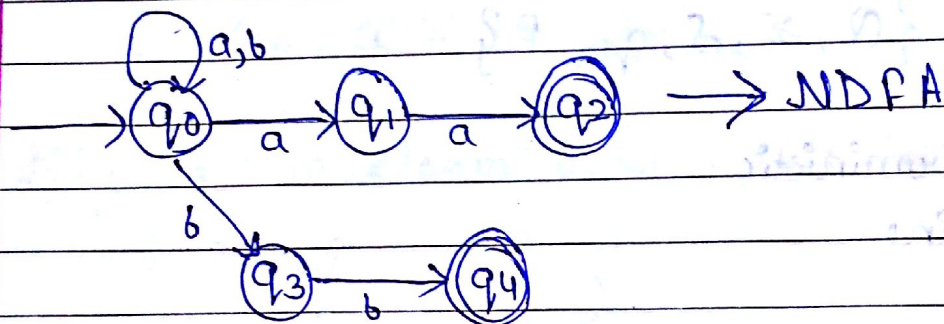
Que $\rightarrow$



Input - 01000

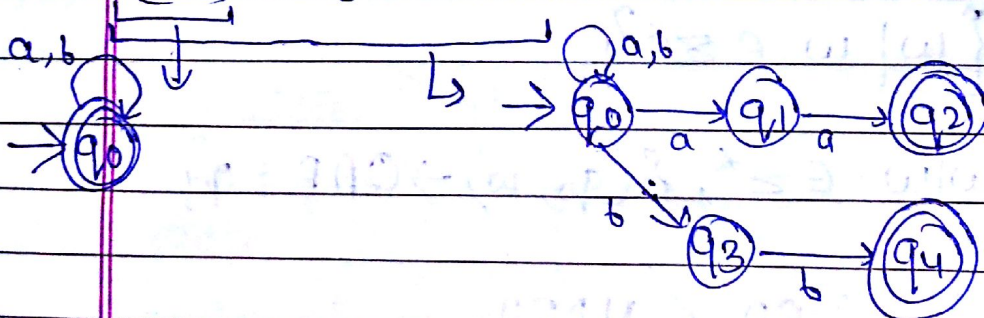


Que $\rightarrow$



a^*bb , b^*aa

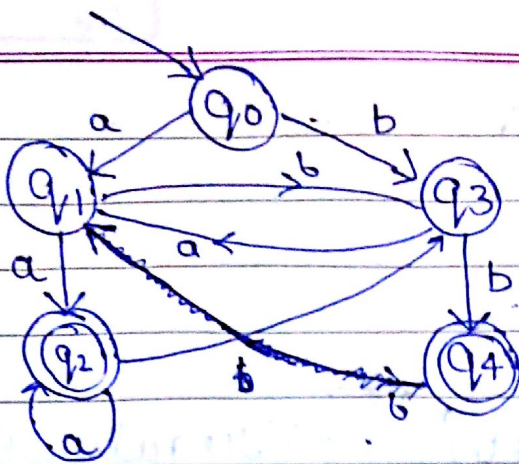
$(a+b)^* (bb+aa)$



Transition table $\div$

State	a	b
$\rightarrow q_0$	$\{q_0, q_1\}$	$\{q_0, q_3\}$
q_1	q_2	$\emptyset$
q_2	$\emptyset$	$\emptyset$
q_3	$\emptyset$	q_4
q_4	$\emptyset$	$\emptyset$

Q2



$(a+b)^* (aa+bb)$

aaabbb

bbbb aa

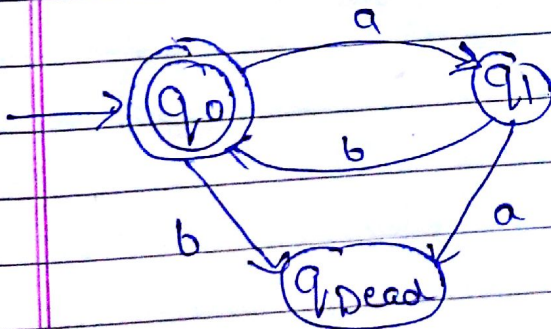
→ To Convert NFA and DFA.

NFA

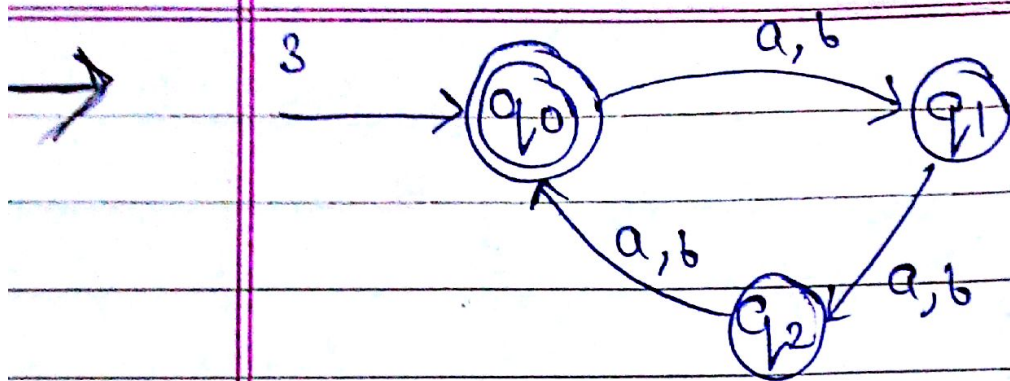
State	0	1
q ₀	{q ₀ , q ₁ }	∅
q ₁	∅	{q ₁ , q ₂ }
q ₂	∅	∅

DFA

q ₀	[q ₀ q ₁]	∅
[q ₀ q ₁]	[q ₀ q ₁]	[q ₁ q ₂]
[q ₁ q ₂]	∅	[q ₁ q ₂]
∅	∅	∅



$(ab)^* abababab.$



$$\Sigma = \{a, b\}$$

$$\Sigma^3 = \begin{matrix} a & a & a \\ b & b & b \\ a & b & b \\ b & a & a \end{matrix}$$

$(a+b)^n$ $n \geq 3$ → regular Expression

→ NFA ← DFA
 Transition table ↔ Regular Expression

CSE 4 projects: wordpres.com

→ Theory of Automata Notes